

# Beer Pong

Investigating  
scenarios and strategies



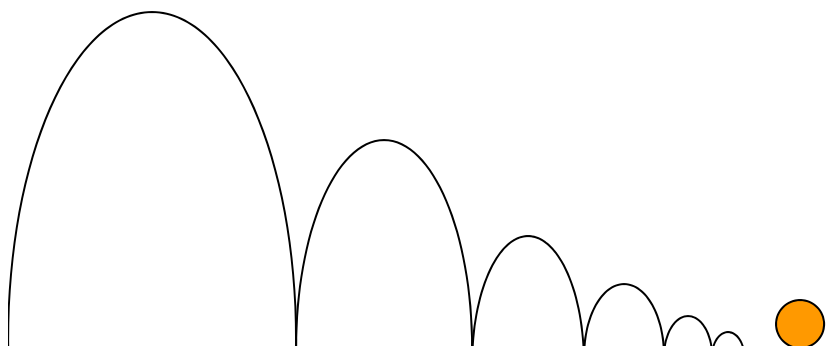
Maureen St Georges  
Scientific Computing | Spring 2007

# TABLE



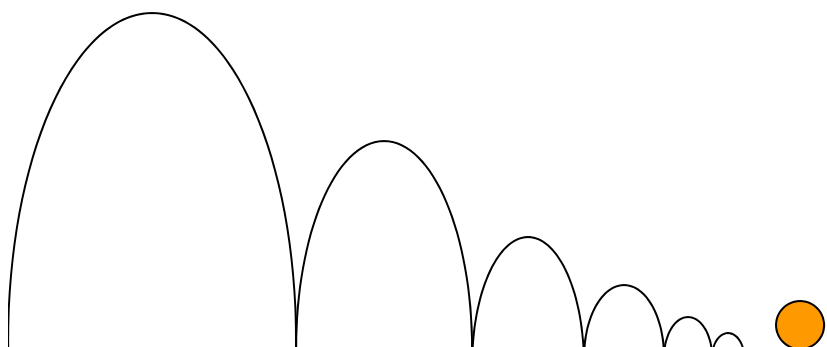
2 feet

8 feet



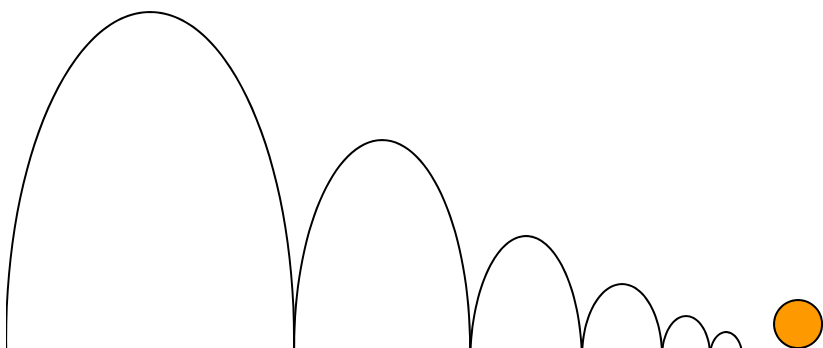
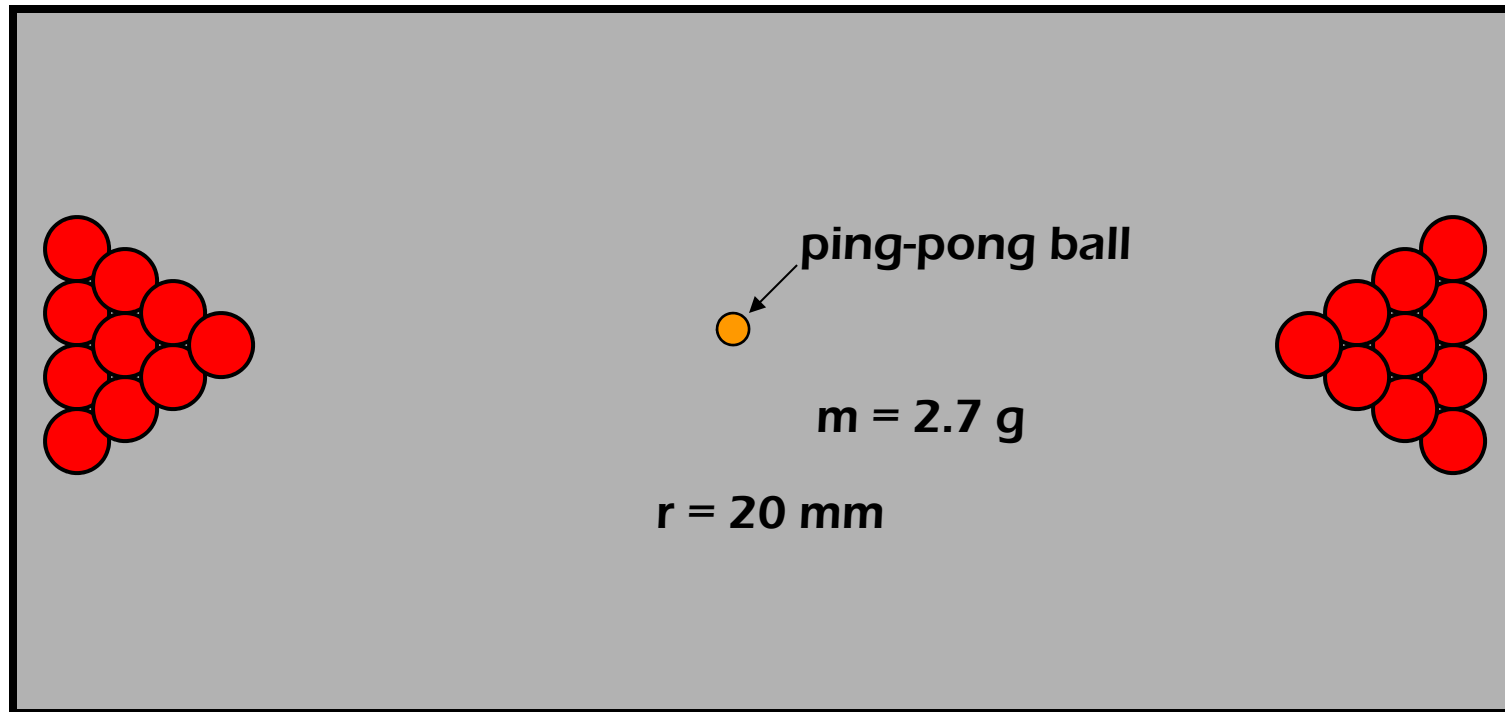
# TARGETS

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## PROJECTILE

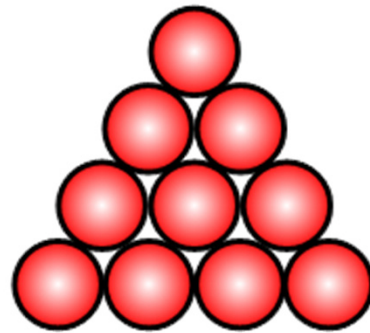
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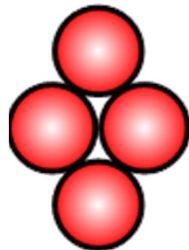
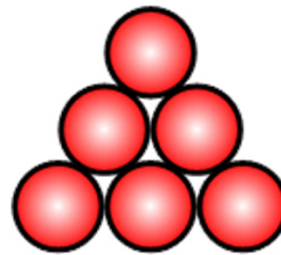
# RACKS

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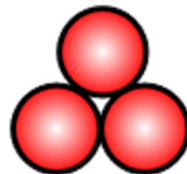
10



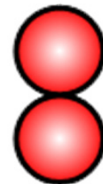
6



4



3

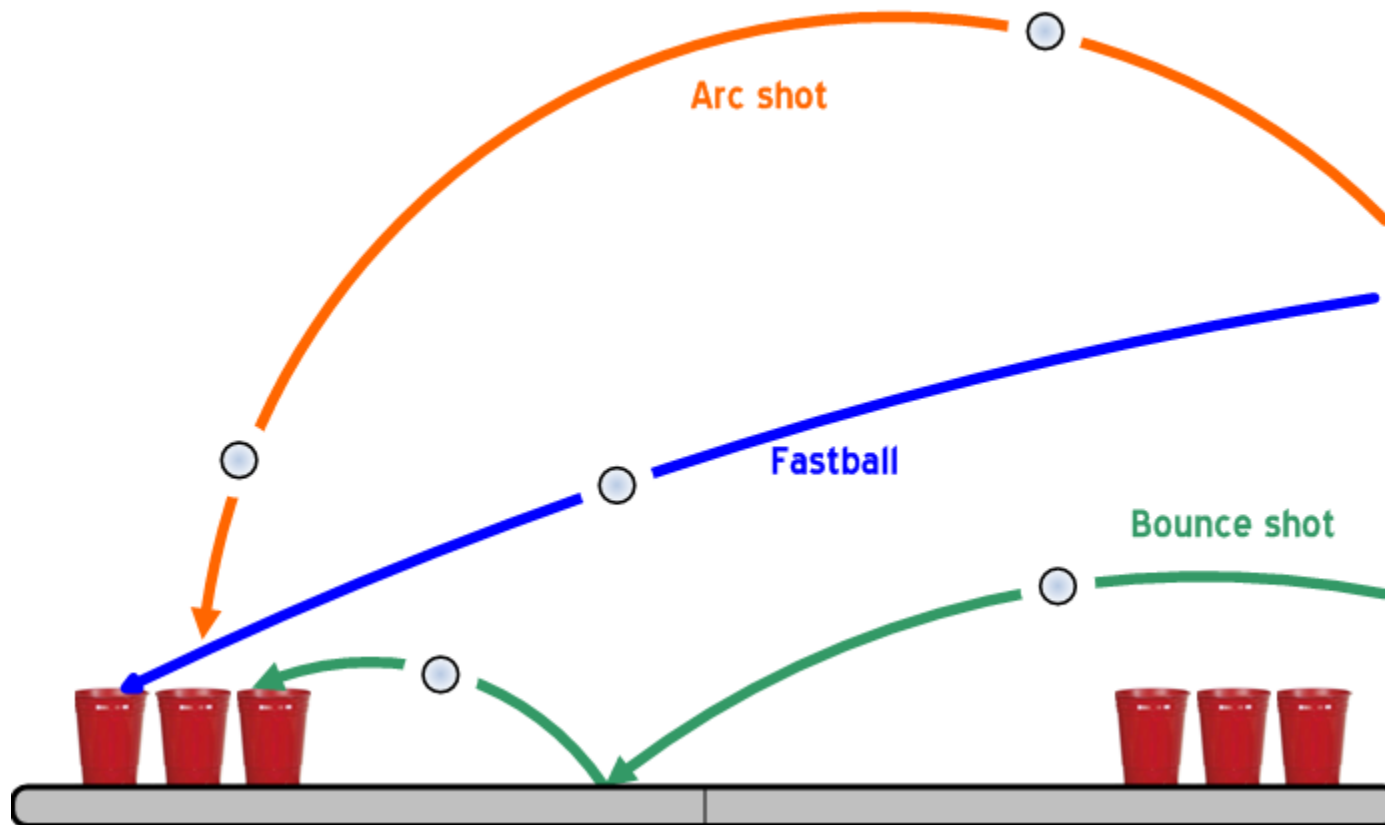


2



1

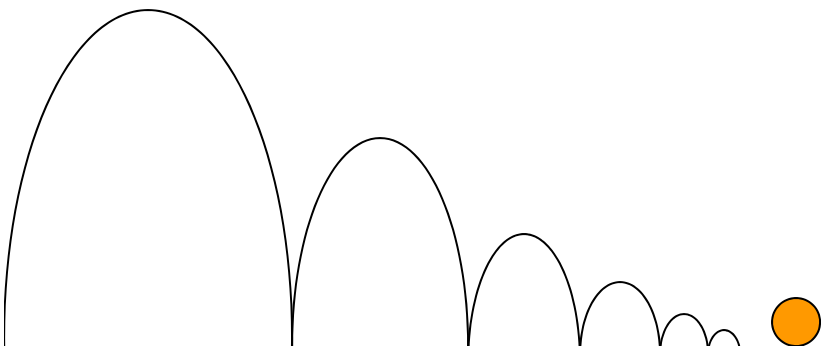
# SHOTS



## GOALS

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- **model projectile motion and bouncing motion of ping-pong ball**
- **explore probabilities of advantageous shots and racks**

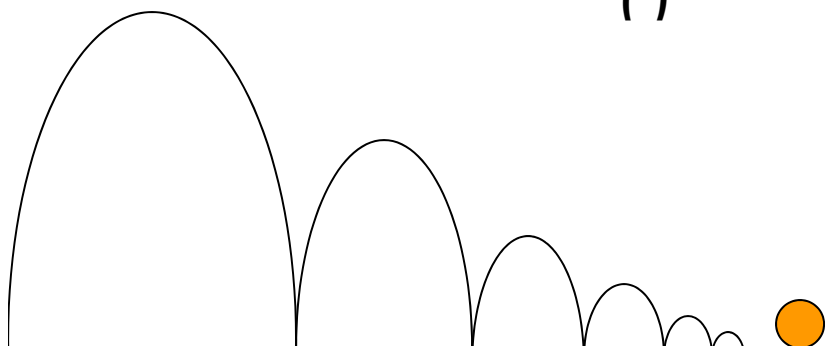


## MODEL

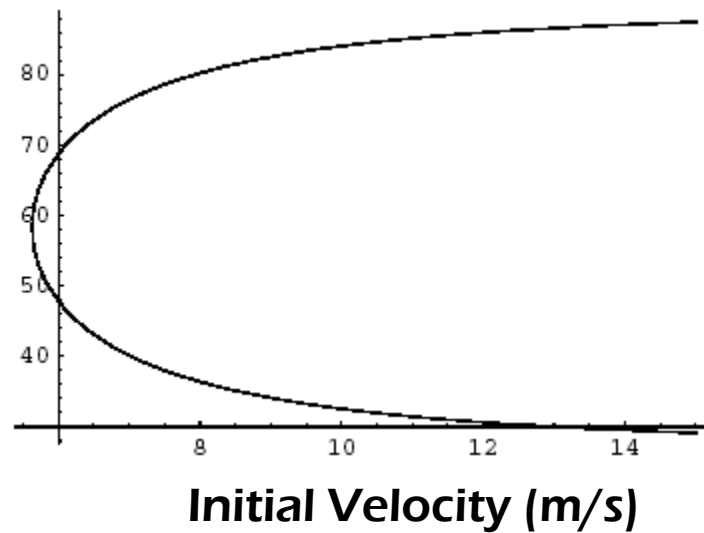
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- Angle necessary to reach a target (x, y) with initial velocity v:

$$\theta = \tan^{-1} \left( \frac{v^2 \pm \sqrt{v^4 - g(gx^2 + 2yv^2)}}{gx} \right)$$



Launch  
Angle  
(°)



## MODEL

---

### ● Velocity adjusted for air resistance:

```
(* Air resistance: *)  
r = 0.03;  
n = 1.8 * 10 ^ (-5);  
k = 6 * Pi * n * r;  
m = 0.0027;
```

$$\text{Vel}[v_, x_] = v * e^{(-k/m * (x/v))};$$

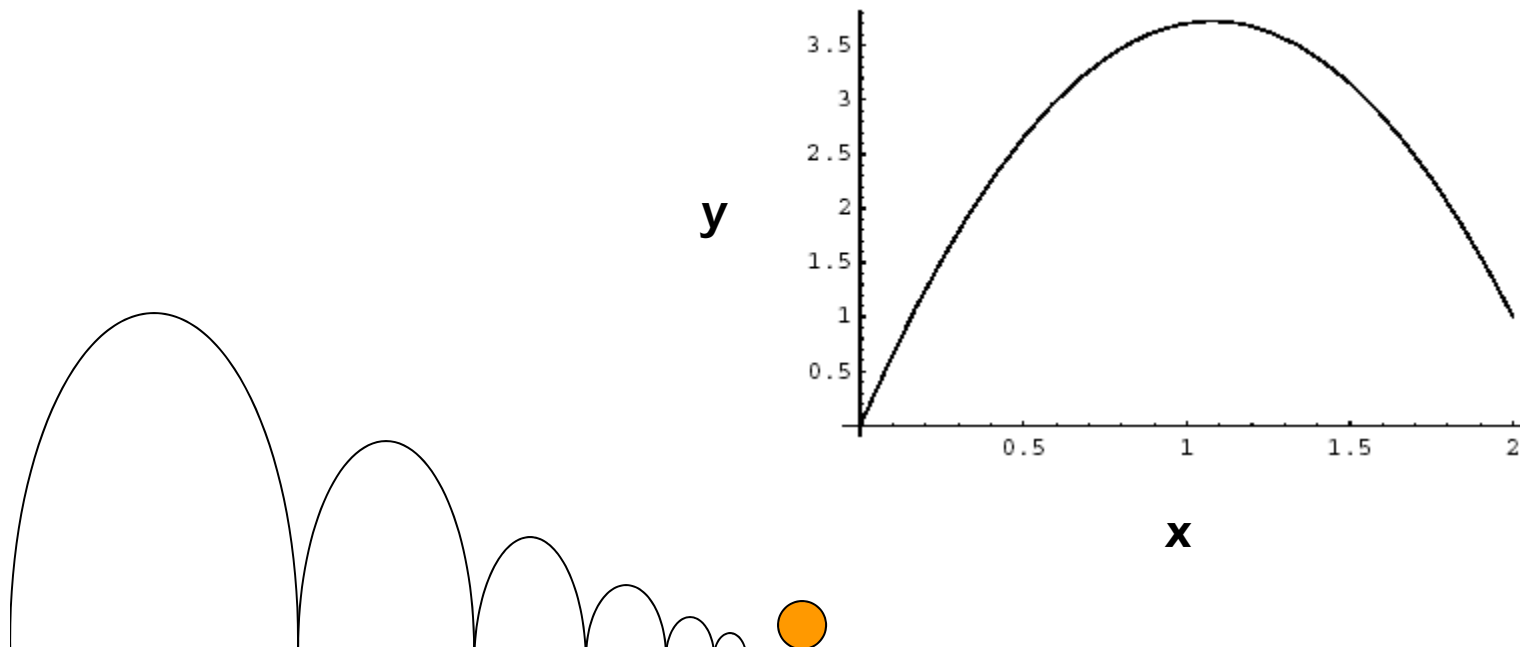


## MODEL

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- Trajectory with initial velocity  $v$  and angle  $\theta$  to reach target  $(x, y)$ :

$$y = x \tan \theta - \frac{gx^2}{2v^2 \cos^2 \theta}$$

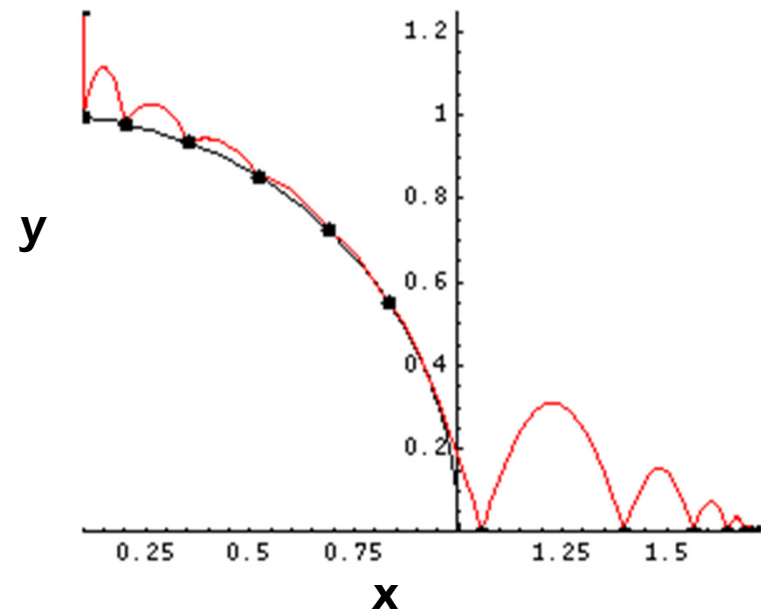


## FUTURE WORK:

- Bouncing & restitution coefficient:

```
restCoef = 0.93;
```

```
vBounce = restCoef * Vel[v, xTarget]
```



**Solution:**

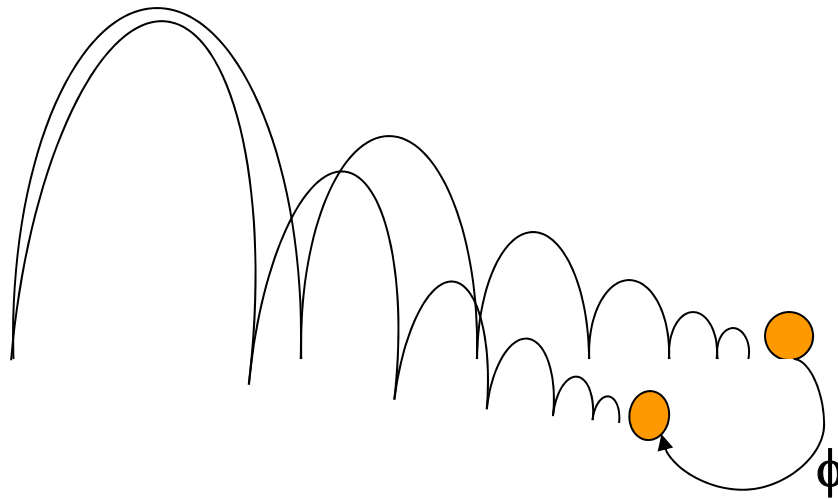
**Mathematica's EventLocator**



## FUTURE WORK

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● 3<sup>rd</sup> dimension,  $\phi$  :



## **FUTURE WORK**

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● explore probabilities:

● racks:

line racks

dense racks

● shots:

arc

bounce



**QUESTIONS?**

**?**

