

An asterisk* denotes that the publication is available online at the ArXiv at <http://front.math.ucdavis.edu/>, or (likely) on someone's webpage (do a web search in Google, for instance).

Combinatorial Convexity

Proof of colorful Caratheodory: [1].

Text on convexity: [2].

Matousek's excellent book at the graduate level has a section on this: [3].

Helly's theorem

A nice section on Helly's theorem and applications: [4].

A new paper on a fractional Helly: [5].

Polytopes

A nice introduction is this chapter: [6]* in the book [7] which is a great overall introduction.

Ziegler's excellent book at the graduate level: [8].

Grübaum's classic text: [9].

Coxeter's classic text on regular polytopes: [10].

Kalai's proof that simple polytopes determined by their graph: [11]*.

Interesting history, nice pictures: [12].

McMullen's upper bound theorem: [13].

Triangulations

My paper on triangulations of cubes: [14]*

Upper bounds for triangulations of a planar point set: [15]*.

The space of triangulations is disconnected: [16]*.

The polytope of pointed pseudo-triangulations: [17]*.

Chamber complexes of polytopes: [18].

Riemann hypothesis for triangulable manifolds: [19].

Combinatorial Fixed Point Theorems and Sperner's Lemma

Cake-cutting and rent-division applications: [20]*.

A polytopal generalization: [21]*.

Another analogue: [22].

Computation and applications to economics: [23].

A different generalization of Sperner's lemma: [24].

^{0*}The MAA's Professional Enhancement Program (PREP) is funded by the NSF (grant DUE-0341481).

Tucker's lemma

The first constructive proof: [25]

Another constructive proof: [26]*.

Cake-cutting applications: [27]*.

Borsuk-Ulam implies Brouwer: [28]*.

Other papers on combinatorial fixed point theorems available at my webpage:

<http://www.math.hmc.edu/~su/papers.html>

Kneser colorings

Joshua Greene's proof of the Kneser conjecture: [29].

Lovasz's famous proof of the Kneser conjecture: [30].

A survey by Björner: [31]*.

A paper by Ziegler on generalized Kneser colorings: [32]*.

Trees

A combinatorial fixed point theorems for trees: my paper will be available at

<http://www.math.hmc.edu/~su/papers.html> later this summer.

The tree metric theorem: [33].

A biologist's book on phylogenies: [34].

Geometry of the space of phylogenetic trees: [35]*.

Tropical Geometry

A nice introduction is a chapter in [36].

Also: [37]*.

Tropical convexity: [38]*.

Rank of a tropical matrix: [39]*.

Tropical halfspaces: [40]*.

See other papers on the ArXiv at

<http://front.math.ucdavis.edu/>.

Lattice point counting and Ehrhart polynomials

Ehrhart's paper: [41].

Coefficients and roots of Ehrhart Polynomials: [42]*.

An application of counting lattice points: [43]*.

A new book by Beck and Robins: see the webpage of Matthias Beck later this summer:

<http://math.sfsu.edu/beck/papers.html>.

Unsolved problems

Book with lots of unsolved problems: [44].

References

- [1] Imre Bárány. A generalization of Carathéodory's theorem. *Discrete Math.*, 40(2-3):141–152, 1982.
- [2] Steven R. Lay. *Convex sets and their applications*. Robert E. Krieger Publishing Co. Inc., Malabar, FL, 1992. Revised reprint of the 1982 original.
- [3] JiříMatoušek. *Lectures on discrete geometry*, volume 212 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, 2002.
- [4] Roger Webster. *Convexity*. Oxford Science Publications. The Clarendon Press Oxford University Press, New York, 1994.
- [5] Imre Bárány and JiříMatoušek. A fractional Helly theorem for convex lattice sets. *Adv. Math.*, 174(2):227–235, 2003.
- [6] Martin Henk, Jürgen Richter-Gebert, and Günter M. Ziegler. Basic properties of convex polytopes. In *Handbook of discrete and computational geometry*, CRC Press Ser. Discrete Math. Appl., pages 243–270. CRC, Boca Raton, FL, 1997.
- [7] Jacob E. Goodman and Joseph O'Rourke, editors. *Handbook of discrete and computational geometry*. CRC Press Series on Discrete Mathematics and its Applications. CRC Press, Boca Raton, FL, 1997.
- [8] Günter M. Ziegler. *Lectures on polytopes*, volume 152 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, 1995.
- [9] Branko Grünbaum. *Convex polytopes*, volume 221 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, second edition, 2003. Prepared and with a preface by Volker Kaibel, Victor Klee and Günter M. Ziegler.
- [10] H. S. M. Coxeter. *Regular polytopes*. Dover Publications Inc., New York, third edition, 1973.
- [11] Gil Kalai. A simple way to tell a simple polytope from its graph. *J. Combin. Theory Ser. A*, 49:381–383, 1988.
- [12] Peter R. Cromwell. *Polyhedra*. Cambridge University Press, Cambridge, 1997. “One of the most charming chapters of geometry”.
- [13] Peter McMullen. The maximum numbers of faces of a convex polytope. *Mathematika*, 17:179–184, 1970.
- [14] Adam Bliss and Francis Edward Su. Lower bounds for simplicial covers and triangulations of cubes.
- [15] Francisco Santos and Raimund Seidel. A better upper bound on the number of triangulations of a planar point set. *J. Combin. Theory Ser. A*, 102(1):186–193, 2003.
- [16] Francisco Santos. A point set whose space of triangulations is disconnected. *J. Amer. Math. Soc.*, 13(3):611–637 (electronic), 2000.

- [17] Günter Rote, Francisco Santos, and Ileana Streinu. Expansive motions and the polytope of pointed pseudo-triangulations. In *Discrete and computational geometry*, volume 25 of *Algorithms Combin.*, pages 699–736. Springer, Berlin, 2003.
- [18] Tatiana V. Alekseyevskaya. Combinatorial bases in systems of simplices and chambers. In *Proceedings of the 6th Conference on Formal Power Series and Algebraic Combinatorics (New Brunswick, NJ, 1994)*, volume 157, pages 15–37, 1996.
- [19] K. S. Sarkaria. A “Riemann hypothesis” for triangulable manifolds. *Proc. Amer. Math. Soc.*, 90(2):325–326, 1984.
- [20] Francis Edward Su. Rental harmony: Sperner’s lemma in fair division. *Amer. Math. Monthly*, 106(10):930–942, 1999.
- [21] Jesus A. De Loera, Elisha Peterson, and Francis Edward Su. A polytopal generalization of Sperner’s lemma. *J. Combin. Theory Ser. A*, 100(1):1–26, 2002.
- [22] Robert M. Freund. Combinatorial analogs of Brouwer’s fixed-point theorem on a bounded polyhedron. *J. Combin. Theory Ser. B*, 47(2):192–219, 1989.
- [23] Michael J. Todd. *The computation of fixed points and applications*. Springer-Verlag, Berlin, 1976. Lecture Notes in Economics and Mathematical Systems, Vol. 124.
- [24] Duane W. DeTemple and Jack M. Robertson. An analog of Sperner’s lemma. *Amer. Math. Monthly*, 83(6):465–467, 1976.
- [25] Robert M. Freund and Michael J. Todd. A constructive proof of Tucker’s combinatorial lemma. *J. Combin. Theory Ser. A*, 30(3):321–325, 1981.
- [26] Timothy Prescott and Francis Edward Su. A Constructive Proof of Ky Fan’s Generalization of Tucker’s Lemma.
- [27] Forest W. Simmons and Francis Edward Su. Consensus-halving via theorems of Borsuk-Ulam and Tucker. *Math. Social Sci.*, 45(1):15–25, 2003.
- [28] Francis Edward Su. Borsuk-Ulam implies Brouwer: a direct construction. *Amer. Math. Monthly*, 104(9):855–859, 1997.
- [29] Joshua E. Greene. A new short proof of Kneser’s conjecture. *Amer. Math. Monthly*, 109(10):918–920, 2002.
- [30] L. Lovász. Kneser’s conjecture, chromatic number, and homotopy. *J. Combin. Theory Ser. A*, 25(3):319–324, 1978.
- [31] A. Björner. Topological methods. In *Handbook of combinatorics, Vol. 1, 2*, pages 1819–1872. Elsevier, Amsterdam, 1995.
- [32] Günter M. Ziegler. Generalized Kneser coloring theorems with combinatorial proofs. *Invent. Math.*, 147(3):671–691, 2002.
- [33] Charles Semple and Mike Steel. *Phylogenetics*. Oxford Univ. Press, 2003.

-
- [34] Joseph Felsenstein. *Inferring Phylogenies*. Sinauer Associates, Inc., 2003.
- [35] Louis J. Billera, Susan P. Holmes, and Karen Vogtmann. Geometry of the space of phylogenetic trees. *Adv. in Appl. Math.*, 27(4):733–767, 2001.
- [36] Bernd Sturmfels. *Solving systems of polynomial equations*, volume 97 of *CBMS Regional Conference Series in Mathematics*. Published for the Conference Board of the Mathematical Sciences, Washington, DC, 2002.
- [37] Jürgen Richter-Gebert, Bernd Sturmfels, and Thorsten Theobald. First steps in tropical geometry.
- [38] Mike Develin and Bernd Sturmfels. Tropical Convexity. AIM 2003-16.
- [39] M. Develin, F. Santos, and B. Sturmfels. On the rank of a tropical matrix. AIM 2003-25.
- [40] Michael Joswig. Tropical Halfspaces.
- [41] E. Ehrhart. Sur un problème de géométrie diophantienne linéaire. II. Systèmes diophantiens linéaires. *J. Reine Angew. Math.*, 227:25–49, 1967.
- [42] M. Beck, J. A. De Loera, M. Develin, J. Pfeifle, , and R. P. Stanley. Coefficients and Roots of Ehrhart Polynomials. AIM 2004-1.
- [43] Matthias Beck, Moshe Cohen, Jessica Cuomo, and Paul Gribelyuk. The number of “magic” squares, cubes, and hypercubes. *Amer. Math. Monthly*, 110(8):707–717, 2003.
- [44] Hallard T. Croft, Kenneth J. Falconer, and Richard K. Guy. *Unsolved problems in geometry*. Problem Books in Mathematics. Springer-Verlag, New York, 1994. Corrected reprint of the 1991 original. *Unsolved Problems in Intuitive Mathematics*, II.